

Bohr's theory of hydrogen atom.

Radius of hydrogen atom.

In a hydrogen atom, an electron having charge - e revolves round the nucleus having charge +e in a circular orbit of radius r.

The force of attraction between the nucleus and the electron is

$$F = \frac{1}{4 \pi \epsilon_0} \frac{e e}{r^2} = \frac{e^2}{4 \pi \epsilon_0 r^2} \dots\dots\dots(1)$$

This force provides the centripetal force for the orbiting energy

i. e. $\frac{e^2}{4 \pi \epsilon_0 r^2} = \frac{m v^2}{r} \dots\dots\dots(2)$

$$m v^2 = \frac{e^2}{4 \pi \epsilon_0 r} \dots\dots\dots (3)$$

According to Bohr's second postulate, $m v r = \frac{n h}{2 \pi}$

$$\therefore v = \frac{nh}{2\pi mr} \dots\dots\dots(4)$$

$$\therefore r = \frac{\epsilon_0 n^2 h^2}{\pi e^2 m} \dots\dots\dots(5) \quad \text{where } n=1,2,3,\dots\dots\dots$$

Bohr's radius

The radius of the innermost orbit (1st orbit) in hydrogen atom is called Bohr's radius.

If $n = 1$ in (5) $r_0 = \frac{\epsilon_0 h^2}{\pi m e^2} = 0.53 \text{ \AA}$

Energy of electron in the Hydrogen atom.

The Kinetic Energy of revolving electron is $KE = \frac{1}{2} mv^2 \dots\dots\dots(6)$

Substituting for mv^2 from (3), $KE = \frac{e^2}{8\pi\epsilon_0 r} \dots\dots\dots(7)$

Potential Energy of electrons is $PE = - \frac{e^2}{4\pi\epsilon_0 r} \dots\dots\dots(8)$

Now total energy, $TE = KE + PE$

i.e. $E = \frac{e^2}{8\pi\epsilon_0 r} + \frac{-e^2}{4\pi\epsilon_0 r} \therefore E = \frac{-e^2}{8\pi\epsilon_0 r} \dots\dots\dots(9)$

Substituting for r from (5); Energy of electron in hydrogen orbit, $E = \frac{-me^4}{8\epsilon_0^2 n^2 h^2} \dots\dots\dots(10)$

Substituting the values of m, e, ϵ_0 and h then $E = \frac{-13.6}{n^2} \text{ eV}$

Energy levels

Ground state (E_1)

It is the lowest energystate in which the electron revolve in the orbit of smallest radius. For ground state,