

READING MATERIAL

- Measures of dispersion are Range, Quartile Deviation, Mean Deviation, Variance.

- Range = Maximum value – Minimum value

- Mean deviation for ungrouped data

$$\text{MD}(\bar{x}) = \frac{\sum_{i=1}^n |x_i - \bar{x}|}{n} \quad \text{MD}(M) = \frac{\sum_{i=1}^n |x_i - M|}{n}$$

- Mean deviation for grouped data

$$\text{MD}(\bar{x}) = \frac{\sum_{i=1}^n |x_i - \bar{x}|}{N} \quad \text{MD}(M) = \frac{\sum_{i=1}^n |x_i - M|}{N}$$

$$\text{Where, } N = \sum_{i=1}^n f_i$$

- Variance and Standard Deviation for ungrouped data

$$\sigma^2(x) = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n} \quad \sigma(x) = \sqrt{\frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n}}$$

- Variance and Standard Deviation of a discrete frequency distribution

$$\sigma^2(x) = \frac{\sum_{i=1}^n f_i (x_i - \bar{x})^2}{N} \quad \sigma(x) = \sqrt{\frac{\sum_{i=1}^n f_i (x_i - \bar{x})^2}{N}}$$

- Variance and Standard Deviation of a discrete frequency distribution

$$\sigma^2(x) = \frac{\sum_{i=1}^n f_i (x_i - \bar{x})^2}{N} \quad \sigma(x) = \frac{1}{N} \sqrt{[N \sum_{i=1}^n f_i x_i^2 - (\sum_{i=1}^n f_i x_i)^2]}$$

- Shortcut method to find Variance and Standard Deviation

$$\sigma = \frac{h^2}{N^2} \left[N \sum_1^n f_i y_i^2 - \left(\sum_1^n f_i y_i \right)^2 \right]$$

$$\sigma = \frac{h}{N} \sqrt{ N \sum_1^n f_i y_i^2 - \left(\sum_1^n f_i y_i \right)^2 }$$

Where,

$$y_i = \frac{x_i - A}{h}$$

- Coefficient of Variation = $\frac{\sigma}{\bar{x}} \times 100$, $\bar{x} \neq 0$

For series with equal means, the series with lesser Standard Deviation is more consistent or less scattered.